



Forced Vibration and Resonance

Name: _____

Class: _____

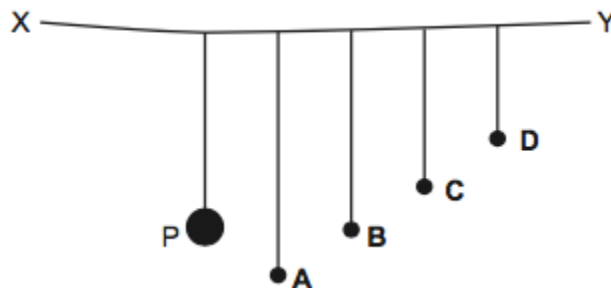
Date: _____

Time: **75 minutes**

Marks: **53 marks**

Comments:

- 1** The diagram shows a string XY supporting a heavy pendulum P and four pendulums **A**, **B**, **C** and **D** of smaller mass.

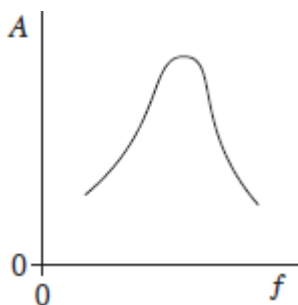


Pendulum P is set in oscillation perpendicular to the plane of the diagram.

Which one of the pendulums, **A** to **D**, then oscillates with the largest amplitude?

(Total 1 mark)

- 2** A periodic force is applied to a lightly-damped object causing the object to oscillate. The graph shows how the amplitude A of the oscillations varies with the frequency f of the periodic force.



Which one of the following statements best describes how the shape of the curve would differ if the damping had been greater?

- A** the curve would be lower at all frequencies
- B** the curve would be higher at all frequencies
- C** the curve would be unchanged except at frequencies above the resonant frequency where it would be lower
- D** the curve would be unchanged except at frequencies above the resonant frequency where it would be higher

(Total 1 mark)

3

A mechanical system is oscillating at resonance with a constant amplitude. Which one of the following statements is **not** correct?

- A** The applied force prevents the amplitude from becoming too large.
- B** The frequency of the applied force is the same as the natural frequency of oscillation of the system.
- C** The total energy of the system is constant.
- D** The amplitude of oscillations depends on the amount of damping.

(Total 1 mark)

4

Which one of the following statements concerning forced vibrations and resonance is correct?

- A** An oscillating body that is not resonating will return to its natural frequency when the forcing vibration is removed.
- B** At resonance, the displacement of the oscillating body is 180° out of phase with the forcing vibration.
- C** A pendulum with a dense bob is more heavily damped than one with a less dense bob of the same size.
- D** Resonance can only occur in mechanical systems.

(Total 1 mark)

5

Which one of the following statements always applies to a damping force acting on a vibrating system?

- A** It is in the same direction as the acceleration.
- B** It is in the same direction as the displacement.
- C** It is in the opposite direction to the velocity.
- D** It is proportional to the displacement.

(Total 1 mark)

6

A body undergoes forced oscillation. Which one of the following will **not** be increased by increasing the amplitude of the oscillatory driving force?

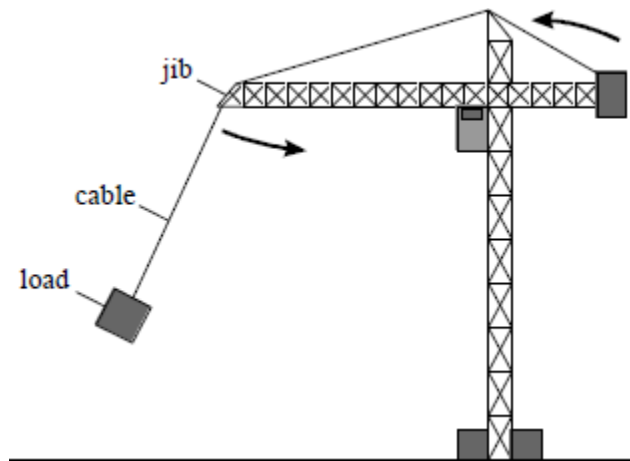
- A the amplitude of the driven oscillation
- B the energy of the driven oscillation
- C the frequency of the driven oscillation
- D the power required to maintain the driven oscillation

(Total 1 mark)

7

The diagram below shows a crane moving a heavy load of mass 1.5×10^3 kg. The mass of the cable is negligible compared with the mass of the load. When the jib moves round and then stops the load swings and behaves like a simple pendulum, undergoing free oscillations. The oscillation has an amplitude of 5.0 m and period of 8.0 s.

the acceleration of free fall, $g = 9.8 \text{ m s}^{-2}$



- (a) (i) Explain briefly the difference between a free and a forced oscillation.

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(2)

- (ii) Calculate the length of the cable.

(2)

- (iii) Determine the maximum acceleration of the load as it swings.

(3)

(iv) Calculate the force on the load that produces this acceleration.

(2)

(b) The total energy of the oscillating load is approximately 12 kJ.

Sketch a graph showing how the **kinetic energy** of the load varies with **time** during one cycle of oscillation. Start your graph at a time when the displacement of the load from the equilibrium position is a maximum. Include appropriate scales on the axes of your graph.

(2)

(Total 11 marks)

8

(a) State what is meant by

(i) a free vibration,

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(ii) a forced vibration.

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(2)

(b) A car and its suspension can be treated as a simple mass-spring system. When four people of total weight 3000 N get into a car of weight 6000 N, the springs of the car are compressed by an extra 50 mm.

(i) Calculate the spring constant, k , of the system.

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(ii) Show that, when the system is displaced vertically and released, the time period of the oscillations is 0.78 s.

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(3)

(c) The loaded car in part (b) travels at 20 m s^{-1} along a road with humps spaced 16 m apart.

(i) Calculate the time of travel between the humps.

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- (ii) Hence, state and explain the effect the road will have on the oscillation of the car.

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(3)
(Total 8 marks)

9

- (a) A vibrating system which is experiencing forced vibrations may show *resonance*.

Explain what is meant by

forced vibrations

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resonance.....

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(3)

- (b) (i) Explain what is meant by *damping*.

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- (ii) What effect does damping have on resonance?

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(2)
(Total 5 marks)

10

To celebrate the Millennium in the year 2000, a footbridge was constructed across the River Thames in London. After the bridge was opened to the public it was discovered that the structure could easily be set into oscillation when large numbers of pedestrians were walking across it.

- (a) What name is given to this kind of physical phenomenon, when caused by a periodic driving force?

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(1)

- (b) Under what condition would this phenomenon become particularly hazardous? Explain your answer.

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(4)

- (c) Suggest **two** measures which engineers might adopt in order to reduce the size of the oscillations of a bridge

measure 1

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measure 2

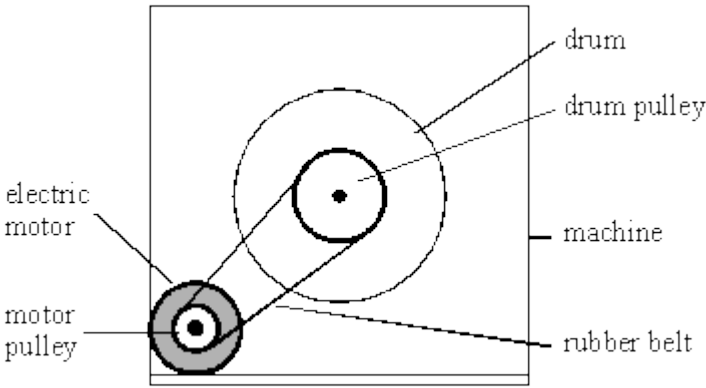
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(2)

(Total 7 marks)

11

An electric motor in a machine drives a rotating drum by means of a rubber belt attached to pulleys, one on the motor shaft and one on the drum shaft, as shown in the diagram below.



(a) The pulley on the motor shaft has a diameter of 24 mm. When the motor is turning at 50 revolutions per second, calculate

(i) the speed of the belt,

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(ii) the centripetal acceleration of the belt as it passes round the motor pulley.

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(5)

- (b) When the motor rotates at a particular speed, it causes a flexible metal panel in the machine to vibrate loudly. Explain why this happens.

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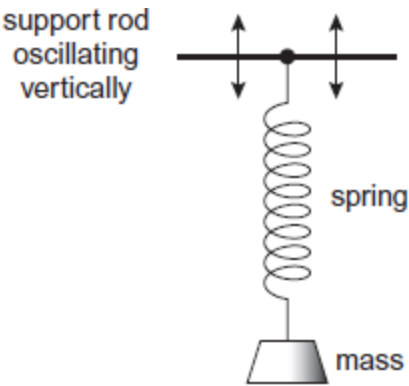
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(2)
(Total 7 marks)

12

- (a) A mass is attached to one end of a spring and the other end of the spring is suspended from a support rod, as shown in **Figure 1**.

Figure 1



The support rod oscillates vertically, causing the mass to perform forced vibrations. Under certain conditions, the system may demonstrate resonance.

Explain in your answer what is meant by forced vibrations and resonance. You should refer to the frequency, amplitude and phase of the vibrations.

forced vibrations

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resonance

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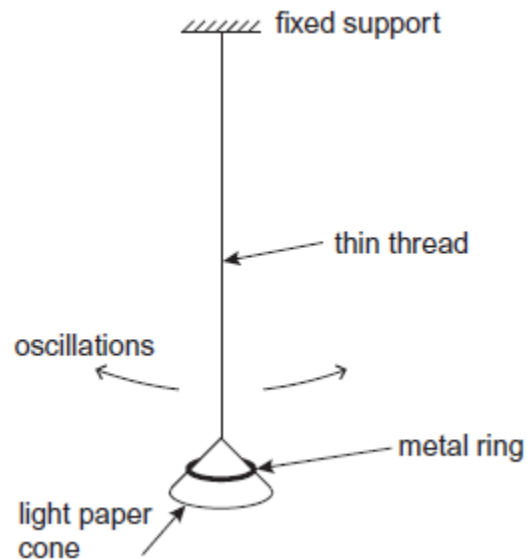
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(4)

- (b) A simple pendulum is set up by suspending a light paper cone (acting as the pendulum bob) on the end of a length of thin thread. A metal ring may be placed over the cone to increase the mass of the bob, as shown in **Figure 2**.

Figure 2



The bob is displaced and released so that it oscillates in a vertical plane. The oscillations are subject to damping.

- (i) Are the oscillations of the pendulum more heavily damped when the cone oscillates with the metal ring on it, when it oscillates without the ring, or does the presence of the ring have no effect on the damping of the oscillations? Tick (✓) the correct answer.

cone oscillates with ring	
cone oscillates without ring	
ring has no effect	

(1)

(ii) Explain your answer to part (i).

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(3)
(Total 8 marks)